

 Information-theoretical bound: for any efficient adversarial algorithm *A*, Pr[*A*(C)=M]=1/2.
 3

Unbreakable Cryptosystems ???

- Almost all of the practical cryptosystems are theoretically breakable given the time and computational resources.
- However, there is one system which is even theoretically unbreakable (perfectly secure): **One-time pad.**

Unbreakable Cryptosystems!!!

- One-time pad requires exchanging key that is as long as the plaintext.
- Security of one-time pad relies on the condition that keys are generated using truly random sources.
- However impractical, it is still being used in certain applications which necessitate very high-level security. Also, the "**masked by the random key**" structure is used everywhere.

Modern Cryptography

- Perfect security: possession of the ciphertext is not adding any new information to what is already known
- There may be useful information in a ciphertext, but if you can't compute it, the ciphertext hasn't really given you anything.

traditional cryptography \Rightarrow

modern cryptography (considering computational difficulties of the adversary)

Modern Cryptography

- What tasks, were the adversary to accomplish them, would make us declare the system insecure?
- What tasks, were the adversary unable to accomplish, would make us declare the scheme secure?
- It is much easier to think about insecurity than security.

traditional cryptography \Rightarrow

modern cryptography (considering provably secure)

Provably Secure Scheme

5

- Provide evidence of computational security by reducing the security of the cryptosystem to some well-studied problem thought to be difficult (e.g., factoring or discrete log).
 - An encryption scheme based on some atomic primitives
 - Take some goal, like achieving privacy via encryption
 - Define the meaning of an encryption scheme to be secure
 - Choose an adversarial model with suitable capability
 - Provide a reduction statement, which shows that the only way to defeat the scheme is to break the underlying atomic primitive

Security Goals of Encryption

Various Security Definitions: 'breakable?'

information-theoretically secure

Computationally secure

& provably secure

- Perfect security
- Plaintext recovery
- Key recovery
- Partial information recovery:
 - Message indistinguishability
 - Semantic Security
- Non-malleability
- Plaintext awareness

Security Goals (cont'd)

- Ex: leaking partial information about "buy" or "sell" a stock n bits, one bit per stock, 1:buy, 0:sell if any one bit were revealed, the adversary knows what I like to do.
- Changing format might avoid the above attack. However, making assumptions, or requirements, on how users format data, how they use it, or what the data content should be, is a bad and dangerous approach to secure protocol designs.

Security Goals (cont'd)

- Simulation paradigm: a scheme is secure if 'whatever a feasible adversary can obtain after attacking it, is also feasibly attainable from scratch'.
- **Semantic security**: Whatever can be obtained from the ciphertext can be computed without the ciphertext
- **Non-malleability**: Given a ciphertext, an adversary cannot produce a different ciphertext that decrypts to meaningfully related plaintext
- **Plaintext awareness**: an adversary cannot create a ciphertext y without knowing its underlying plaintext x

Adversary Models for Encryption

- Ciphertext Only
- Known Plaintext
- Chosen Plaintext
- Non-adaptive Chosen Ciphertext
- Adaptive Chosen Ciphertext

Security Goals for Signature

- Total break : key recovery
- Universal forgery : finding an efficient equivalent algorithm to produce signatures for arbitrary messages
- Selective forgery : forging the signature for a particular message chosen a priori by the attacker
- Existential forgery : forging at least one signature

11

stingent

9

Adversary Models for Signature

- Key-only attack : no-message attacks
- Known-message attack
- Generic chosen-message attack : non-adaptive, messages not depending on public key
- **Directed chosen-message attack** : nonadaptive, messages depending on public key
- Adaptive chosen-message attack : messages depending on the previously seen signatures

13

15

Secure Multiparty Protocols

- Secure multiparty protocol: A group of n participants, each provides a secrect input x_i, want to compute jointly a function f_i(x₁, x₂, ..., x_n) for each participant while keeping their individual input/output secret to that person.
- Security Notion: Whatever can be obtained by a group of participants and the adversary during a real world protocol can also be calculated in the ideal model in which a trusted party helps every participant reaching his functional and security goals.

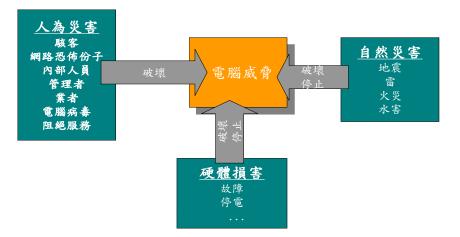
資訊安全的定義

資訊安全:利用各種方法及工具
 以保護靜態資訊(電腦安全)或
 動態資訊(網路安全)

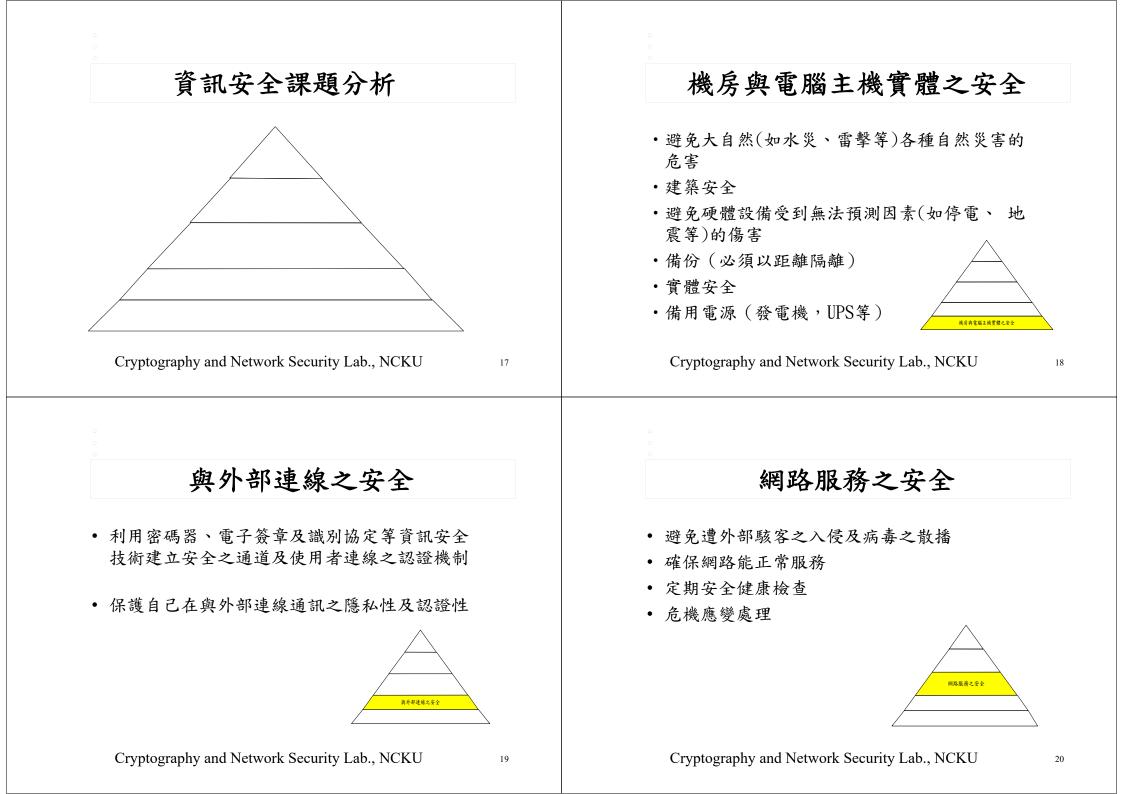


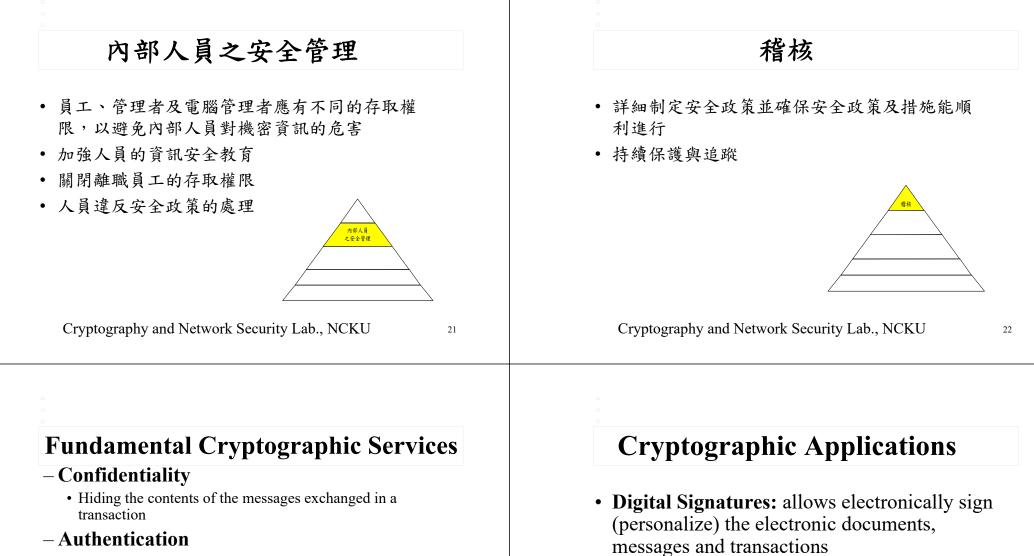


from Cryptography and Network Security Lab., NCKU



powerful





• Ensuring that the origin of a message or the identity is correctly identified

– Integrity

• Ensuring that only authorized parties are able to modify computer system assets and transmitted information

– Non-repudiation

• Requires that neither of the authorized parties deny the aspects of a valid transaction

- Identification / authentication: replace password-based authentication methods with more powerful (secure) techniques.
 - Identification: presenting the unique identity
 - Authentication: associate the individual with his unique identity by something he knows, something he possesses and some specific features of him

Cryptographic Applications

- **Key Establishment:** To communicate a key to your correspondent (or perhaps actually mutually generate it with him) whom you have never physically met before.
- Secret Sharing: Distribute the parts of a secret to a group of people who can never exploit it individually.
- Zero Knowledge Proof: Peggy proves to Victor that she has a particular knowledge without letting Victor learn the knowledge throught the interaction.

Cryptographic Applications

- E-commerce: carry out the secure transaction over an insecure channel like Internet.
- E-cash / E-contract
- E-voting / E-auction
- Games
- Anonymous secret broadcast and tracing
- Stenography (digital watermarking)
- Software protection (IPR)
- Crypto currency & Blockchain

26

Focus of this course

- Analysis of the fundamental primitives and protocols
- Security of the fundamental primitives and protocols

Why Staying in This Class???

- Most of the time in the future you won't be coding the cryptography primitives.
- You will be using these cryptography primitives (as they are from the software libraries or packages).
- Why do you need to stay in this class to understand the background materials of these primitives?

Why Staying in This Class???

- CATCHES: the usage of these primitive has to follow strict security notions
 - insecure SSL mechanism ==> TLS
 - 2002 MSIE SSL implementation faults
 - most textbook's plain
 RSA and ElGamal
 system is insecure
 without preprocessing



29

Why Staying in This Class???

- Standards would be established on most cryptographic primitives. These primitives will be at your disposal when you design your application systems.
- You need to understand clearly these primitives in order to design any customized secure protocol.
- You need to follow the 'provably security' methodology to base your protocols on the security guarantees of the underlying primitives.

Why Staying in This Class???

- Double DES
- Symmetric encryption with ECB mode
- Chosen ciphertext attacks on CBC / OFB / CFB / Counter mode of DES/AES
- Subliminal channels
- Signature scheme without non-repudiation
- SSH (Secure SHell) Authentication & Encryption
- SSL Authentication

30

Aspects of Modern Cryptography

- One way function assumption
- Model adversaries such that they need to solve computationally intractable problems
- Refined security definitions
- Provably secure methodology
- Reduce intractability assumptions
- Reduce trust assumptions
- Reduce physical assumptions

Quantum Computer

- History
 - back to 2000, 4-qubit machines
 - 2011, D-Wave's 128-qubit machine, 2013, 512-qubit machine
 - 2019 IBM's 53-qubit quantum computer
 - 2019 Google's Sycamore, 72-qubit machine
- Interesting physical phenomenons at the atomic level
 - Uncertainty Principle: position and velocity of an object cannot be measured exactly at the same time
 - Quantum Entanglement: Two far-away particles are inextricably linked, and whatever happens to one immediately affects the other.

33

Post Quantum Cryptography

- Lattice-based Cryptography Ring-LWE Signature, NTRU, Fully Homomorphic Enc.
- Multivariate Cryptography
- Hash-based Cryptography Merkle Signature
- Code-based Cryptography McEliece
- Quantum Computation Theory

Quantum Computing

- Bennett and Brassard 1984
 - Quantum key distribution: perfectly secure that Alice and Bob will notice any evesdropping
- Peter Shor 1994
 - Both integer factoring and discrete log problems can be solved in probabilistic polynomial time (actually linear) if the quantum computer of sufficient qubits (e.g 2048) were built successfully
- Grover 1996
 - $O(\sqrt{n})$ quantum algorithm for searching an n-item unsorted database. This allow quantum computer to solve NP-complete problems in polynomial time

Complexity Classes

- P: problems that can be solved by an algorithm with computation complexity O(p(n)) ex. Bubble sort O(n²) Quick sort O(n logn)
 - there are many problems which are not P
 - ex. 2ⁿ knapsack(subset sum)
 - n! Travelling Salesman Problem (TSP) unsolvable halting problem
- NP: decision problems that have solutions which can be verified by a polynomial time algorithm (problems that might still have polynomial time solutions) ex. decision-TSP, Satisfiability (SAT), knapsack, Factoring, ...

35

Complexity Classes (cont'd)

• NP-hard:

- all NP problems have a poly-time mapping reduction to them. Once you have a poly-time solution for any one of NP-hard problems, you have a poly-time solution for every NP problem. However, an NP-hard problem itself might not be an NP problem. Usually, a problem is NP-hard if you find an NPcomplete problem that reduces to it.
- ex. search-TSP, SVP, TQBF, halting problem (unsolvable)
- NP-complete:
 - Def 1: NP problems, all NP problems can be reduced to them
 - Def 2: NP problems, to which SAT can be reduced
 - Def 3: NP \cap NP-Hard
 - ex. SAT, decision-TSP, G3C, Knapsack ...

37

Complexity Classes (cont'd)

reduction

 $P_1 \leq P_2$

means "if P_2 were solved by a poly-time algorithm \mathcal{A} , P_1 can also be solved by calling poly-times of the same algorithm \mathcal{A} "

 or equivalently "if P₁ is unsolvable polynomially, P₂ is also unsolvable polynomially".